

# Welcome!

STATS 2020: Re-envisioning Intro Stats for a New Generation

Applying GAISE in Practice

November 22, 2019

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\***G**uidelines for **A**ssessment and **I**nstruction in **S**tatistics **E**ducation

# How much do you know about GAISE ?

## How much do you know about the GAISE report?

Nothing whatsoever - that's why I'm here! **A**

A tiny bit. Knew it had something to do with Stat Education. **B**

Read some of it once upon a time. **C**

Quite familiar; can judge consistency with [my] course **D**

# Today's Plan:

## Nuts and Bolts of GAISE

**What ?**

**Who?**

**Where?**

**When?**

**Why?**

*Then a little more what and how, and finally an activity to demonstrate...*

# Nuts and Bolts about **GAISE**

**Guidelines for Assessment and Instruction in Statistics Education.**

**What:** Goals and Recommendations for teaching statistics. Then it gives piles of examples.

# Nuts and Bolts about **GAISE**

**Guidelines for Assessment and Instruction in Statistics Education.**

**Who:** American Statistical Association (ASA)  
with AMATYC endorsement

**Where:** Fully available on the web (via ASA) !  
Just google “GAISE” and you’ll get to it!

[www.amstat.org/files/pdfs/GAISE/GaiseCollege\\_Full.pdf](http://www.amstat.org/files/pdfs/GAISE/GaiseCollege_Full.pdf)

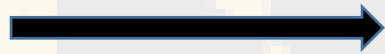
# Nuts and Bolts about **GAISE**

## Guidelines for Assessment and Instruction in Statistics Education.

**When: 2016**

1992

The “Cobb Report”  
published in an MAA  
Volume “Heeding the  
Call for Change”



2003:

ASA funded development  
of Guidelines

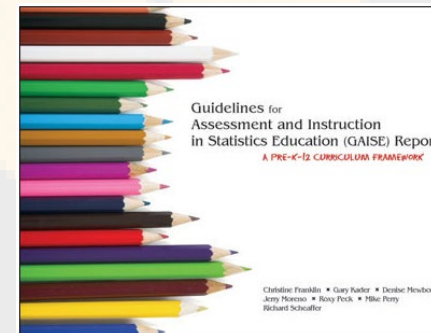


Introductory College  
Statistics - 2005

COLLEGE REPORT



PreK-12 Curriculum - 2007



**Revised, 2016**

Guidelines for Assessment and Instruction  
in Statistics Education (GAISE)  
College Report 2016

# Nuts and Bolts about the **GAISE College Reports** **Guidelines for Assessment and Instruction in Statistics Education.**

**Who:** American Statistical Association (ASA)  
with AMATYC endorsement

**Really – *who?***

*2016 Committee:*

Robert Carver (Stonehill College), Michelle Everson, co-chair (The Ohio State University), John Gabrosek (Grand Valley State University), Nicholas Horton (Amherst College), **Robin Lock** (St. Lawrence University), Megan Mocko, co-chair (University of Florida), **Allan Rossman** (Cal Poly – San Luis Obispo), Ginger Holmes Rowell (Middle Tennessee State University), **Paul Velleman** (Cornell University), Jeffrey Witmer (Oberlin College), and Beverly Wood (Embry-Riddle Aeronautical University)

[**Original**] 2005 writing team:

Martha Aliaga, **George Cobb**, Carolyn Cuff, **Joan Garfield** (chair), Rob Gould, **Robin Lock**, Tom Moore, **Allan Rossman**, Bob Stephenson, **Jessica Utts**, **Paul Velleman**, Jeff Witmer

# Nuts and Bolts about **GAISE**

**Guidelines for Assessment and Instruction in Statistics Education.**

**Why:** Generally a need to cement and disseminate the ideas from statistics education movement that took off in the 90s.

Changes in Content and Enrollment Trends in Stats Education over Decades



# Nuts and Bolts about **GAISE**

## **Guidelines for Assessment and Instruction in Statistics Education.**

**Why:** Generally a need to cement and disseminate the ideas from statistics education movement that took off in the 90s.

Changes in Content and Enrollment Trends in Stats Education over Decades

**College Enrollment:** Introductory Statistics at Two-Year colleges as percent of Calculus Enrollments\*:

Year	1966	1970	1980	1990	2000	2010
Percent	10	19	27	52	74	Over 100

**High School, AP Statistics exam takers\*\*:**

Year	1997	1998	1999	2000	2004	2015
Exam-takers	7500	15000	25000	35000	>65000	Near 200,000

\* '66, 70, 80, 90 from <http://jse.amstat.org/v1n1/cobb.html> and '00 and '10 from [https://www.amstat.org/asa/files/pdfs/GAISE/GaiseCollege\\_Full.pdf](https://www.amstat.org/asa/files/pdfs/GAISE/GaiseCollege_Full.pdf), p. 28. 9

\*\* 1997-2000 numbers from GAISE, 2005 report, p. 7; 2004, 2015 numbers from GAISE, 2016, p. 29

# Nuts and Bolts about the **GAISE**

## **Guidelines for Assessment and Instruction in Statistics Education.**

**Why:** Generally a need to cement and disseminate the ideas from statistics education movement that took off in the 90s.

**Changes in Content and Enrollment Trends in Stats Education over Decades**

Early on: 1992 “Cobb Report”:

1. Emphasize Statistical Thinking
2. More Data and concepts, Less Theory and fewer recipes
3. Foster active learning

More recently, pertaining to “revising” **College Report from 2005 to 2016...**

1. Attend to “changes in...statistics education and statistical practice since 2005”
2. Informed by outreach to stat education community and by stat education literature



**Re-upping of 2005 recommendations**

# GAISE College Report 2016

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# 2016 GAISE Report **recommendations:**



1. Teach **statistical thinking**.
2. Focus on **conceptual** understanding.

WHAT



3. Integrate **real data** with a **context** and **purpose**.
4. Foster **active learning**.
5. Use technology to explore concepts and analyze data.
6. Use assessments to improve and evaluate student learning.

HOW



# 2016 GAISE Report recommendations:

1. Teach **statistical thinking**.

- Teach statistics as an **investigative process** of problem-solving and **decision-making**.
- Give students experience with **multivariable** thinking.

2. Focus on conceptual understanding.

3. Integrate **real data** with a **context** and purpose.

4. Foster **active learning**.

5. Use technology to explore concepts and analyze data.

6. Use assessments to improve and evaluate student learning.

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# “Realistic Expectations while setting Aspirational Goals”:

1. Teach statistical thinking.
  - Teach statistics as an investigative process of problem-solving and decision-making.
  - Give students experience with multivariable thinking.
2. Focus on conceptual understanding.
3. Integrate real data with a context and purpose.
4. Foster active learning.
5. Use technology to explore concepts and analyze data.
6. Use assessments to improve and evaluate student learning.

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**Pages 12-23: Each recommendation is explained and followed by a bulleted list of “Suggestions for teachers.”**

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Substantially  
expanded and  
revised from '05

# 1. Teach statistical thinking.

*Why this recommendation?*

- Teach statistics as an investigative process of problem-solving and decision-making.

An analogy to a class in carpentry...

*In week 1 of the carpentry course (**statistics**), we learned to use various kinds of planes (**summary statistics**). In week 2, we learned to use different kinds of saws (**graphs**). Then, we learned about using hammers (**confidence intervals**). Later, we learned about the characteristics of different types of wood (**tests**). By the end of the course, we had covered many aspects of carpentry (**statistics**).*

*But I wanted to learn how to **build a table** (**collect and analyze data to answer a question**) and I never learned how to do that. (GAISE 2016, p. 13)*

# Suggestions for Topics that Might be **Omitted** from Introductory Statistics Courses

- Probability theory
- Constructing plots by hand
- Basic statistics
- Drills with z-, t-,  $\chi^2$ , and F-table
- Advanced training on a statistical software program.



# Suggestions for Topics that Might be **Omitted** from Introductory Statistics Courses

- **Probability theory** – *“GAISE goals and recommendations can be met **without** [basic probability and rules about random variables, with binomial as special case]”*
- Constructing plots by hand
- **Basic statistics** – brief coverage suggested as review, due to place that statistics now plays in Common Core SS, e.g., pie charts, scatter plots, histograms, means, medians
- **Drills with z-, t-,  $\chi^2$ , and F-table:** *“These skills are no longer necessary and do not reflect modern statistical practice. Apps that perform the lookup (not limited to a finite list of df values) [are ubiquitous]... This shift makes it unnecessary to examine students on their ability to use these tables, so they can usually be dispensed with on exams.”*
- Advanced training on a statistical software program.

# GAISE in practice...

“Statistics can be thought of as the science of **learning from data**, so the context of the data becomes an integral part of the problem-solving experience” (p. 17)

*An Activity to demonstrate some GAISE what's and how's in action...*

# Investigation: Pick Two Cubes

Consider the **game of chance**:

- Put four cubes in a bag, 2 of one color, and 2 of another color.
- Two cubes get pulled out without looking.
- If they are the **same**, one player wins, and if they are **different**, the other player wins.
- *It does not matter who pulls the cubes!*

# Investigation: Pick Two Cubes Game

Is the game *fair*?

*Are the two cubes equally likely to come up same color as they are to come out different colors?*

*What do you predict?*

*How can we investigate this?*

Collect data – all groups collect the same way. How so?

- Groups of 2 or 3: Play a **game of 10 rounds**, recording “same” or “different” for each pull. *Mix well between rounds!*
- At the end of a game, find the **proportion** of “same” color outcomes.
- Play two or more games of 10.

# Investigation: Pick Two Cubes Game

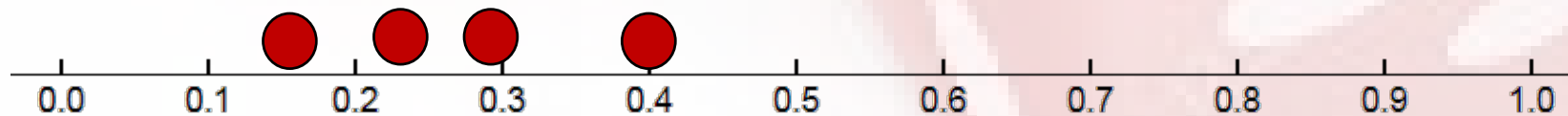
- What's the variable of interest each time we pull out of the bag?
- For a 10-round game, focus on the proportion of a particular outcome.

Revisit your prediction— is it a fair game?  
Why?/Why not?



Proportion of “same color” pulls in a **10**-round game

How might we expect these distributions to compare?



Proportion of “same color” pulls in a **20**-round game

Wish we had loads more data, don't you?

How can we do that?

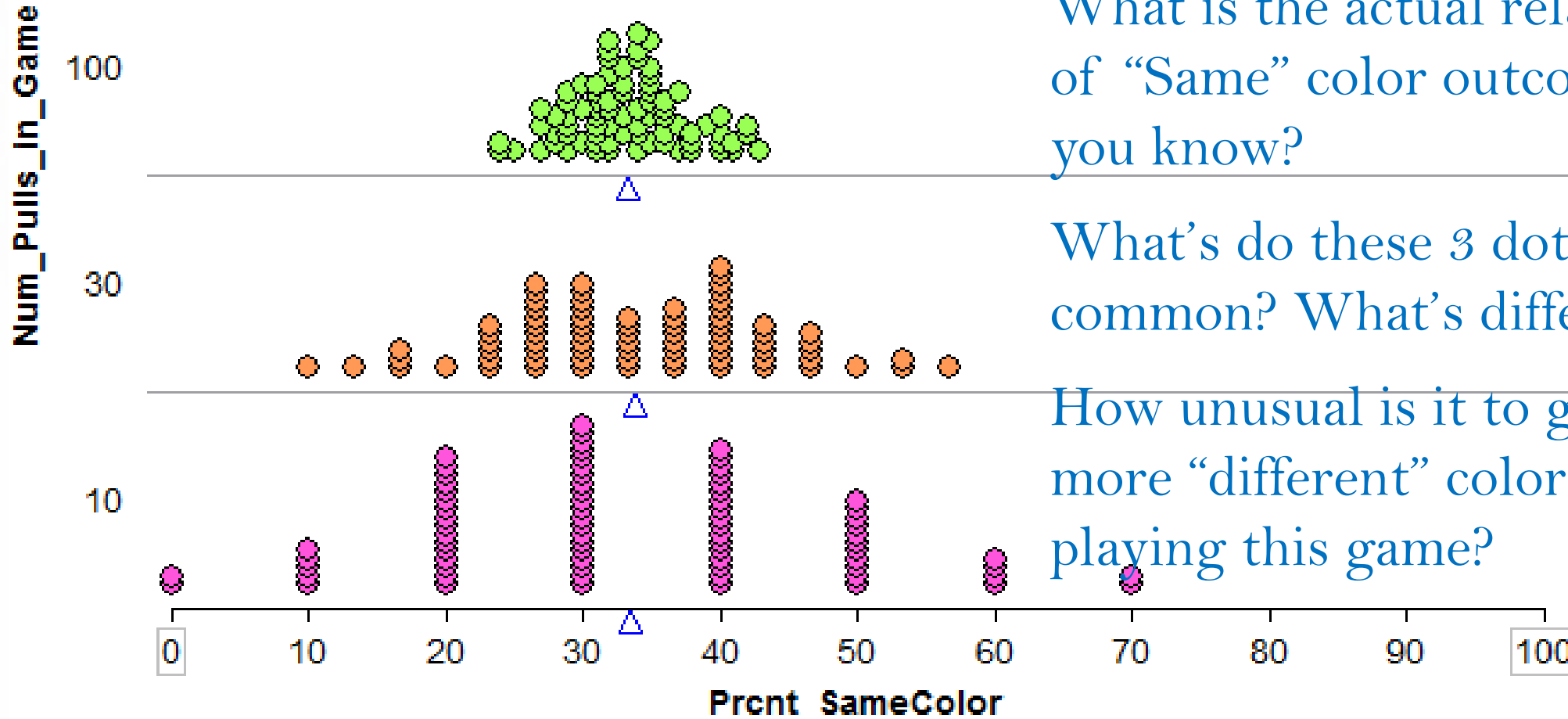
**Simulations!!**

# Investigation: Pick Two Cubes Game



## A computer simulation...

GreenYellow 2, 2 average\_Stat2020.tp



### Main take-aways:

What is the actual relative frequency of “Same” color outcome? How do you know?

What’s do these 3 dotplots have in common? What’s different?

How unusual is it to get 50% or more “different” color cubes when playing this game?

# Investigation: Pick Two Cubes Game

Straight outta GAISE...

## Recommendation 1: Teach statistical thinking

Teach statistics as an **investigative process** of problem-solving

- “Discuss the research question that guided the study, the collection and the analysis of the results...”
- “Begin most examples...classifying variables as categorical or quantitative, and consider... use of random sampling...”
- “Use technology...to explore and visualize data ...”

## Recommendation 2: Focus on conceptual understanding

- “View the primary goal as to discover and apply concepts.”

*Which concepts would you say were covered?*

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# Investigation: Pick Two Cubes Game

Straight outta GAISE...

## Recommendation 3: Integrate real data w/context and purpose

- “Use real data...to enliven class.”
- “Use data with a context as the catalyst for exploration, generating the questions, and informing interpretations.”

## Recommendation 4: Foster Active Learning

- “Consider student need for physical exploration prior to use of computer simulation.”
- “Encourage predictions from students about results... before analyzing data”

## Recommendation 5: Use technology to explore concepts and analyze data

- “Perform simulations to illustrate abstract concepts”

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# Investigation: Pick Two Cubes Game

Straight outta GAISE...

**From Appendix C: Desirable Characteristics of Class Activities, p. 43-45**

- **Data Relevance** – real data collected in real-time by students to answer a question (if only arguably compelling)
- **Design Decisions and Data Collection** – Students helped design method of collection
- **Teamwork** – Employed both to collect data and think/pair/share ideas about what will happen or why things are happening

Go forth, mine GAISE, then *mind* GAISE!

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