

The Future of Intro Stat: More Accessible, More Effective, More Relevant, More Fun!

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STATS 2020 Baltimore, MD November 22nd, 2019 There is a revolution going on in this course, across the country and across all types of institutions

Driven by

TECHNOLOGY!!!

Potential to dramatically enhance student enjoyment and student success!

Intro Stats: Not This

Consider two events A and B, and assume that P(A) = 0.6 and P(B) = 0.5 and $P(A \cap B) = 0.2$. Find $P(A \cup B)$.

Intro Stats: Not This



Intro Stats: Not This



Intro Stats: But This

Are mosquitoes more attracted to beer drinkers? Are the youngest kids in a class more likely to be diagnosed with ADHD? Does leaving a light on at night affect weight? Is there a "commitment" gene? Does diet cola leach calcium out of the system? Does drinking red wine boost metabolism? Il p pnes aff t b Dc 5 r bn fror A lia <u>n</u> ity? re lik 🕰 att ck after ful Ar s n futer Wr printe k Uan f /ad o_____XiI__le ?___ Ddledle Does tagging penguins for identification purposes harm them? Does turning up the music in a bar increase beer consumption? Are city dwellers more likely to have mood and anxiety disorders? Can dogs smell cancer in humans? Does sexual frustration increase the desire for alcohol? How broadly do experiences of parents affect their future children? What percent of college professors consider themselves "above average" teachers? AND SO ON!

What's Out?

Computing statistics by hand

Drawing graphs by hand

Probability rules

Discrete probability distributions

Abstract random variables

What's In? 2016 ASA GAISE Guidelines:

- 1. Teach statistical thinking.
- 2. Focus on **conceptual understanding**.
- 3. Integrate **real data** with a context and purpose.
- 4. Foster active learning.
- 5. Use **technology** to explore concepts and analyze data.
- 6. Use **assessments** to improve and evaluate student learning.

Ways to Change

1. Make everything about real data

Focus on Real Data

Topics of the day:

- Two-way tables
- Graphical displays for two categorical variables
- Difference in proportions

Question of the Day

Is cat ownership related to Schizophrenia?



https://www.youtube.com/watch?v=ahd9Cr0U8XU

Statistics: Unlocking the Power of Data

Lock⁵

Ways to Change

- 1. Make everything about real data
- 2. Reduce tedious "by-hand" work and let **technology** do the heavy-lifting

Rely on technology



STATISTICAL SOFTWARE!!

Larger, real datasets!

More exciting!

Interpretation!

Ways to Change

- 1. Make everything about real data
- 2. Reduce tedious "by-hand" work and let **technology** do the heavy-lifting
- 3. Focus on interpretation and **concepts**

Interpretation and concepts



Ways to Change

- 1. Make everything about real data
- 2. Reduce tedious "by-hand" work and let **technology** do the heavy-lifting
- 3. Focus on interpretation and **concepts**
- 4. Improve conceptual understanding and reduce reliance on prerequisites with simulation-based inference

Simulation-Based Inference



TABLE B: #-DISTRIBUTION CRITICAL VALUES

		. Tail probability p											
ďf	.25	.20	.15	.10	.05	.025	.02	.01	.005	.0025	.001	.000	
1	1.000	1.376	1.963	3.078	6.314	12.71	15.89	31.82	63.66	127.3	318.3	636.	
2	.816	1.061	1.386	1.886	2.920	4.303	4.849	6.965	9.925	14.09	22.33	31.6	
3	.765	.978	1.250	1.638	2.353	3,182	3.482	4.541	5.841	7.453	10.21	12.9	
4	.741	.941	1.190	1.533	2.132	2.776	2.999	3.747	4.604	5.598	7.173	8.61	
5	.727	.920	1.156	1.476	2.015	2.571	2.757	3.365	4.032	4.773	5.893	6.86	
6	.718	.906	1.134	1.440	1.943	2.447	2.612	3.143	3.707	4.317	5.208	5.95	
7	.711	.896	1.119	1.415	1.895	2.365	2.517	2.998	3.499	4.029	4.785	5.40	
8	.706	.889	1.108	1.397	1.860	2.306	2.449	2.896	3.355	3.833	4.501	5:04	
9	.703	.883	1.100	1.383	1.833	2.262	2.398	2.821	3.250	3.690	4.297	4,78	
10	.700	.879	1.093	1.372	1.812	2.228	2.359	2.764	3.169	3.581	4.144	4.58	
11	.697	.876	1.088	1.363	1.796	2.201	2.328	2.718	3.106	3.497	4.025	4.43	
12	.695	.873	1.083	1.356	1.782	2.179	2.303	2.681	3.055	3.428	3.930	4.31	
13	.694	.870	1.079	1.350	1.771	2.160	2.282	2.650	3.012	3.372	3.852	4.22	
14	.692	.868	1.076	1.345	1.761	2.145	2.264	2.624	2.977	3.326	3.787	- 4.14	
15	.691	.866	1.074	1.341	1.753	2.131	2.249	2.602	2.947	3.286	3.733	4.07	
16	.690	.865	1.071	1.337	1.746	2.120	2.235	2.583	2.921	3.252-	3.686	4.01	
17	.689	.863	1.069	1.333	1.740	2.110	2.224	2.567	2.898	3.222	3.646	3.96	
18	.688	.862	1.067	1.330	1.734	2,101	2.214	2.552	2.878	3.197	3.611	3.92	
19	.688	.861	1.066	1.328	1.729	2.093	2.205	2.539	2.861	3.174	3.579	3.88	
20	.687	.860	1.064	1.325	1.725	2.086	2.197	2.528	2.845	3.153	3.552	3.85	
21	.686	.859	1.063	1.323	1.721	2.080	2.189	2.518	2.831	3.135	3.527	3.81	
22	.686	.858	1.061	1.321	1.717	2.074	2.183	2.508	2.819	3.119	3.505	3.79	
23	.685	.858	1.060	1.319	1.714	2.069	2.177	2.500	2.807	3.104	3.485	3.76	
24	.685	.857	1.059	1.318	1.711	2.064	2.172	2.492	2.797	3.091	3,467.	3.74	
25	.684	.856	1.058	1.316	1.708	2.060	2.167	2.485	2.787	3.078	3,450	3.72	
26	.684	.856	1.058	1.315	1.706	2.056	2.162	2,479	2.779	3.067	3.435	3,70	
27	.684	.855	1.057	1.314	1.703	2.052	2.158	2.473	2.771	3.057	3,421	3,69	
28	.683	.855	1.056	1.313	1.701	2.048	2.154	2.467	2.763	3.047	3.408	3.67	
29	.683	.854	1.055	1.311	1.699	2.045	2.150	2.462	2.756	3.038	3.396	3.65	
30	.683	.854	1.055	1.310	1.697	2.042	2.147	2.457	2.750	3.030	3.385	3.64	
40	.681	.851	1.050	1.303	1.684	2.021	2.123	2.423	2.704	2.971	3.307	3.55	
50	.679	.849	1.047	1.299	1.676	2.009	2.109	2.403	2.678	2.937	3.261	3,49	
60	.679	.848	1.045	1.296	1.671	2.000	2.099	2.390	2.660	2.915	3.232	3,46	
80	.678	.846	1.043	1.292	1.664	1.990	2.088	2.374	2.639	2.887	3.195	3.41	
100	.677	.845	1.042	1.290	1.660	1.984	2.081	2.364	2.626	2.871	3,174	3.39	
000	.675	.842	1.037	1.282	1.646	1.962	2.056	2.330	2.581	2.813	3.098	3.30	
00	.674	.841	1.036	1.282	1.645	1.960	2.054	2.326	2.576	2.807	3.091	3.29	
	50%	60%	70%	80%	90%	95%	96%	98%	99%	99.5%	99.8%	99.95	



Example: Beer & Mosquitoes

<u>Question</u>: Does consuming beer attract mosquitoes?

Experiment: 25 volunteers drank a liter of beer, 18 volunteers drank a liter of water Randomly assigned! Mosquitoes were caught in traps as they approached the volunteers.¹

¹ Lefvre, T., et. al., "Beer Consumption Increases Human Attractiveness to Malaria Mosquitoes," *PLoS ONE*, 2010; 5(3): e9546.

Number of Mosquitoes Beer mean Water mean Beer Water = 23.6= 19.224.38 Beer mean – Water mean 🗲 Two possible explanations: Beer attracts mosquitos No difference; random chance \bullet Does drinking beer actually attract mosquitoes or is the difference just due to random chance?

Number of Mosquitoes

<u>Beer</u>	<u>Water</u>				
27	21				
20	22				
21	15				
26	12				
27	21				
31	16				
24	19				
19	15				
23	24				
24	19				
28	23				
19	13				
24	22				
29	20				
20	24				
17	18				
31	20				
20	22				
25					
28					
21					
27					

21 18 20 What kinds of results would we see, just by random chance, if there were no difference between beer and water?

We can simulate to find out!!!

Number of Mosquitoes

<u>Beer</u>					<u>Water</u>
27	27	19	21	24	21
20	20	24	18	19	22
21	21	29	20	23	15
26	26	20	21	13	12
27	27	27	22	22	21
31	31	31	15	20	16
24	24	20	12	24	19
19	19	25	21	18	15
23	23	28	16	20	24
24	24	21	19	22	19
28	28	27	15		23
19					13
24					22
29					20
20					24
17					18
31					20
20					22
25					
28					
21					
27					
21					
18					
20					

 Assume no difference (beer/water doesn't matter).

Mimic random chance: Re-randomize the 43 values into two groups of 25 and 18

Number of Mosquitoes

<u>Beer</u>					<u>Water</u>
	27	19	21	24	
	20	24	28	19	
	2 4	29	20	23	
	2 5	20	21	13	
	207	27	29	22	
	24	31	25	20	
	31	20	18	24	
	19	25	<u>22</u>	18	
	28	28	<u>10</u>	20	
	24	21	29	22	
	2 \$	27	2 9		
	21		20		
	18		27		
	15		21		
	21		17		
	16		24		
	28		28		
	22				
	19				
	27				
	20				
	23				
	22				
	21				

 Assume no difference (beer/water doesn't matter).

- Mimic random chance: Re-randomize the 43 values into two groups of 25 and 18
- 3. Compute the beer mean minus the water mean for this simulated sample.

$$\bar{x}_B - \bar{x}_W = -0.84$$

4. Do this thousands of times!

We need technology!!

STATKEY!

www.lock5stat.com/statkey

Free, online, works on all platforms, easy to use

Randomization Dotplot of $\overline{x}_1 - \overline{x}_2$, Null hypothesis: $\mu_1 = \mu_2$



Beer and Mosquitoes The Conclusion!

The results seen in the experiment are very unlikely to happen just by random chance (less than 1 out of 1000!)

We have strong evidence that drinking beer does attract mosquitoes!

Another Look at Beer/Mosquitoes

1. Check conditions

2. Which formula?

5. Which theoretical distribution?

TABLE B: #-DISTRIBUTION CRITICAL VALUES



3. Calculate numbers and plug into formula

$$t = \frac{23.6 - 19.22}{\sqrt{\frac{4.1^2}{25} + \frac{3.7^2}{18}}}$$

4. Chug with calculator

t = 3.680.0005 < p-value < 0.001

					Thi	l probabi	lity p			- /		1040
ďť	.25	.20	.15	.10	.05	.025	.02	.01	.005	.0023	.001	.000
1	1.000	1.376	1.963	3.078	6.314	12.71	15.89	31.82	63.66	127.3	318.2	626.
2	.816	1.061	1.386	1.886	2.920	4.303	4.849	6.965	9.925	14.09	22.33	31.6
3	.765	.978	1.250	1.638	2.353	3.182	3.482	4.541	5.841	7.453	10.21	12.9
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11	.697	.876	1.088	1.363	1.796	2.201	2.328	2.718	3.106	3.497	4,025	4.43
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14	.692	.868	1.076	1.345	1.761	2.145	2.264	2.624	2.977	3.326	3.787	4.14
15	.691	.866	1.074	1.341	1.753	2.131	2.249	2.602	2.947	3.286	3.733	4.07
16	600	265	1.071	1 3 3 7	1 7.46	2 120	3 235	2 592	2 021	3 363	3 696	4.01
17	.689	.863	1.069	1.333	1.740	2.110	2.224	2.567	2.898	3.222	3.646	3.96
10	.080	.502	1.007	1.330	1.734	2.101	2.219	2.332	2.8/8	3.19/	3.011	3.92
19	.088	.501	1.064	1.328	1.729	2.093	2.205	2.539	2.801	3.174	3.579	3.88
20	160.	.800	1.069	1.343	1.763	2.080	2.197	2.528	2.845	3.153	3.552	3.85
22	060.	.839	1.003	1.323	1.721	2.080	2.169	2.518	2.831	3.135	3.527	3.81
22	393.	929	1.060	1.341	1.714	2.0/4	2.183	2.508	2.819	3.119	3.303	3.79
23	.085	.0.30	1.050	1.319	1.714	2.009	2.177	2.500	2.807	3.104	3.485	3.76
25	600.	.031	1.059	1.316	1.702	2.004	2.1/2	2.492	2.191	3.091	3.467.	3.74
25	.034	.620	1.058	1.310	1.708	2.060	2.167	2.455	2.787	3.078	3.450	3.72
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	V			LJ) - V	a	IU	Ci	•••	
50	.679	.849	1.047	1.299	1.676	2.009	2.109	2.403	2.678	2.937	3.261	3.49
60	.679	.848	1.045	1.296	1.671	2.000	2.099	2.390	2.660	2.915	3.232	3.46
80	.678	.846	1.043	1.292	1.664	1.990	2.088	2.374	2.639	2.887	3.195	3.41
100	.677	.845	1.042	1.290	1.660	1.984	2.081	2.364	2.626	2.871	3.174	3.39
	.675	.842	1.037	1.282	1.646	1.962	2.056	2.330	2.581	2.813	3.098	3.30
1000	100 A	841	1.036	1.282	1.645	1.960	2.054	2.326	2.576	2.807	3.091	3.29
1000	.674	1042	11909									
1000 	.674	60%	70%	80%	90%	95%	96%	98%	99%	99.5%	99.8%	99.99

p-value: The chance of obtaining a statistic as extreme as that observed, just by random chance, if the null hypothesis is true

Randomization Dotplot $\mu_1 = \mu_2$, number othesis: $\mu_1 = \mu_2$



Conclusions are the same, but the process is very different!

"Students' approach to p-values ... was procedural ... and [they] did not attach much meaning to p-values"

-- Aquilonius and Brenner, "Students' Reasoning about P-Values", SERJ, November 2015

Simulation-Based Inference

- Visual!
- Intuitive!
- Easily incorporates active learning!
- Ties directly to key concepts!
- Same process for all parameters!
- More generalizable!
- No theoretical distributions! No formulas! No formal probability!
- No algebra!!!



Why is there a push now to change?

Technology!!!

We now have the technological power to do thousands of simulations quickly and easily.

Ways to Change

- 1. Make everything about real data
- 2. Reduce tedious "by-hand" work and let **technology** do the heavy-lifting
- 3. Focus on interpretation and **concepts**
- 4. Improve conceptual understanding and reduce reliance on prerequisites with **simulation-based inference**
- 5. Embrace the power of **data visualization** and multivariable thinking

2016 GAISE Guidelines

- 1. Teach statistical thinking.
 - Teach statistics as an investigative process of problem-solving and decision making.
 - Give students experience with multivariable thinking.
- 2. Focus on conceptual understanding.
- 3. Integrate real data with a context and purpose.
- 4. Foster active learning.
- 5. Use technology to explore concepts and analyze data.
- 6. Use assessments to improve and evaluate student learning.

Data Visualization



Score









2016: The Hottest Year



OK Cupid Data



Scatterplot



Scatterplot: Add a 3rd Variable!



Scatterplot: Add a 4th Variable!


But we want more!

Make it INTERACTIVE!

Make it DYNAMIC!

www.gapminder.com/tools

Hans Rosling's 200 Countries, 200 Years, 4 Minutes The Joy of Stats – BBC Four

US Population by Age and Sex

NEXT AMERICA

Percent of U.S. Population by Age Group, 1950-2060



PEW RESEARCH CENTER

www.pewresearch.org/next-america/#Two-Dramas-in-Slow-Motion



A whole class of global warming data visualizations

Obesity* in U.S. Adults: 1985 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)







Obesity* in U.S. Adults: 1986 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)





Obesity* in U.S. Adults: 1987 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)





Obesity* in U.S. Adults: 1988 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)





Obesity* in U.S. Adults: 1989 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)





Obesity* in U.S. Adults: **1990** (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)





Obesity* in U.S. Adults: 1991 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



Obesity* in U.S. Adults: 1992 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



Obesity* in U.S. Adults: 1993 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



Obesity* in U.S. Adults: 1994 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



Obesity* in U.S. Adults: 1995 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



Obesity* in U.S. Adults: 1996 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



Obesity* in U.S. Adults: 1997 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



___ No Data ___<10% ___10%–14% ___15-19% ___≥20%

Obesity* in U.S. Adults: 1998 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



___ No Data ___<10% ___10%–14% ___15-19% ___≥20%

Obesity* in U.S. Adults: 1999 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



___ No Data ___<10% ___10%–14% ___15-19% ___≥20%

Obesity* in U.S. Adults: 2000 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



Obesity* in U.S. Adults: 2001 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



___ No Data ___<10% ___10%–14% ___15-19% ___ 20-24% ___≥25%

Obesity* in U.S. Adults: 2002 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



____ No Data ____<10% ___10%–14% ___15-19% ____20-24% ____≥25%

Obesity* in U.S. Adults: 2003 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



___ No Data ___<10% ___10%–14% ___15-19% ___ 20-24% ___≥25%

Obesity* in U.S. Adults: 2004 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



____No Data ____<10% ___10%–14% ___15-19% ____20-24% ____≥25%

Obesity* in U.S. Adults: 2005 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



No Data <10% 10%−14% 15-19% 20-24% 25-29% ≥30%

Obesity* in U.S. Adults: 2006 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



No Data

Obesity* in U.S. Adults: 2007 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



No Data

Obesity* in U.S. Adults: 2008 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



____No Data ____<10% ___10%-14% ___15-19% ____20-24% ____25-29% ____≥30%

Obesity* in U.S. Adults: 2009 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



No Data

Obesity* in U.S. Adults: 2010 (*BMI ≥30, or ~ 30 lbs. overweight for 5' 4" person)



No Data

Obesity Trends* Among U.S. Adults BRFSS, 1990, 2000, 2010

(*BMI ≥30, or about 30 lbs. overweight for 5' 4" person)



Two Different Visualizations



http://stateofobesity.org/adult-obesity/

Data Visualization

- Visual!
- Intuitive!
- Engages right brain and creativity!
- Emphasizes multivariable thinking!
- Exposes a new world of possibilities!
- Engaging for students of all math abilities!
- Fun!! (for students and teachers!)
- Lots of good examples here: <u>www.personal.psu.edu/klm47/visualization.htm</u>



Why is there a push now to change?

Technology!!! We now have the technological ability to collect large datasets and to visualize them.

The Future of Intro Stat: More Accessible

Fewer Prerequisites

NONE of this requires algebra!!!

=> accessible to more students, and more students can succeed!

Also not required:

- Formal probability
- Theoretical distributions
- Test statistic or standard error formulas

The Future of Intro Stat: More Effective
More Effective!



More Effective!



The Future of Intro Stat: More Relevant

REAL DATA!!

Intro Stats for Who?

Students who are good at math

 This is one of only three courses the <u>2015 MAA Curriculum</u> <u>Guide</u> recommends for all math majors

Students who are not good at math

 A <u>randomized experiment (!)</u> found students needing remedial math had greater success in intro stats than college algebra



- Students who plan to become math teachers
 - Simulation-based inference recommended by <u>SET 2015</u>
- Students in fields that analyze data
 - User disciplines love the emphasis on real data
- Students taking stats for general education
 - "statistical thinking will one day be as necessary for efficient citizenship as the ability to read and write." - H.G. Wells

The Future of Intro Stat: More Fun!

Consider two events A and B, and assume that P(A) = 0.6 and P(B) = 0.5and $P(A \cap B) = 0.2$. Find $P(A \cup B)$.







We have strong evidence that drinking beer does attract mosquitoes!



	Tail probability p											
ď	1 .25	.20	.15	.10	.05	.025	.02	.01	.005	.0025	.001	.000
	1.00	1.376	1.963	3.078	6.314	12.71	15.89	31.82	63.66	127.3	318.3	636
-	.810	1.061	1.386	1.886	2.920	4.303	4.849	6.965	9.925	14.09	22.33	31.6
1.5	76	.978	1.250	1.638	2.353	3.182	3.482	4.541	5.841	7.453	10.21	12.9
4	.741	.941	1.190	1.533	2.132	2.776	2.999	3.747	4.604	5.598	7.173	8.61
	.72	.920	1.156	1.476	2.015	2.571	2.757	3.365	4.032	4.773	5.893	6.86
1	. 718	.906	1.134	1.440	1.943	2.447	2.612	3.143	3.707	4.317	5.208	5.95
7	.711	.896	1.119	1.415	1.895	2.365	2.517	2.998	3.499	4.029	4.785	5.40
8	.706	.889	1.108	1.397	1.860	2.306	2.449	2.896	3.355	3.833	4.501	5:04
5	.703	.883	1.100	1.383	1.833	2.262	2.398	2.821	3.250	3.690	4.297	4.78
10	.700	.879	1.093	1.372	1.812	2.228	2.359	2.764	3.169	3.581	4.144	4.58
11	.697	.876	1.088	1.363	1.796	2.201	2.328	2.718	3.106	3.497	4.025	4.43
12	.695	.873	1.083	1.356	1.782	2.179	2.303	2.681	3.055	3.428	3.930	4.31
13	.694	.870	1.079	1.350	1.771	2.160	2.282	2.650	3.012	3.372	3.852	4.22
14	.692	.868	1.076	1.345	1.761	2.145	2.264	2.624	2.977	3.326	3.787	-4.14
15	.691	.866	1.074	1.341	1.753	2.131	2.249	2.602	2.947	3.286	3.733	4.07
16	.690	.865	1.071	1.337	1.746	2.120	2.235	2.583	2.921	3.252-	3.686	4.01
17	.685	.863	1.069	1.333	1.740	2.110	2.224	2.567	2.898	3.222	3.646	3.96
18	.688	.862	1.067	1.330	1.734	2.101	2.214	2.552	2.878	3.197	3.611	3.92
15	.688	.861	1.066	1.328	1.729	2.093	2.205	2.539	2.861	3.174	3.579	3.88
20	.687	.860	1.064	1.325	1.725	2.086	2.197	2.528	2.845	3.153	3.552	3.85
21	.686	.859	1.063	1.323	1.721	2.080	2.189	2.518	2.831	3.135	3.527	3.81
22	.686	.858	1.061	1.321	1.717	2.074	2.183	2.508	2.819	3.119	3.505	3.79
23	.685	.858	1.060	1.319	1.714	2.069	2.177	2.500	2.807	3.104	3.485	3.76
24	685	.857	1.059	1.318	1.711	2.064	2.172	2.492	2.797	3.091	3.467.	3.74
25	.684	.856	1.058	1.316	1.708	2.060	2.167	2.485	2.787	3.078	3.450	3.72
26	.684	.856	1.058	1.315	1.706	2.056	2.162	2.479	2.779	3.067	3.435	3.70
27	.684	.855	1.057	1.314	1.703	2.052	2.158	2.473	2.771	3.057	3.421	3.69
28	.683	.855	1.056	1.313	1.701	2.048	2.154	2,467	2.763	3.047	3.408	3.67
29	.683	.854	1.055	1.311	1.699	2.045	2.150	2.462	2.756	3.038	3.396	3.65
30	.683	.854	1.055	1.310	1.697	2.042	2.147	2.457	2.750	3.030	3.385	3.64
40	.681	.851	1.050	1.303	1.684	2.021	2.123	2.423	2.704	2.971	3.307	3.55
50	.679	.849	1.047	1.299	1.676	2.009	2.109	2.403	2.678	2.937	3.261	3.494
60	.679	.848	1.045	1.296	1.671	2.000	2.099	2.390	2.660	2.915	3.232	3.46
80	.678	.846	1.043	1.292	1.664	1.990	2.088	2.374	2.639	2.887	3.195	3.416
100	.677	.845	1.042	1.290	1.660	1.984	2.081	2.364	2.626	2.871	3.174	3.390
1000	.675	.842	1.037	1.282	1.646	1.962	2.056	2.330	2.581	2.813	3.098	3.300
•	.674	.841	1.036	1.282	1.645	1.960	2.054	2.326	2.576	2.807	3.091	3.29
	50%	60%	70%	80%	90%	95%	96%	98%	99%	99.5%	39.8%	99.95

Ways to Change

- 1. Make everything about real data
- 2. Reduce tedious "by-hand" work and let **technology** do the heavy-lifting
- 3. Focus on interpretation and **concepts**
- 4. Improve conceptual understanding and reduce reliance on prerequisites with **simulation-based inference**
- 5. Embrace the power of **data visualization** and multivariable thinking

The Future of Intro Stats

More accessible More effective More relevant More fun!



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